### 5.111 Lecture Summary #17

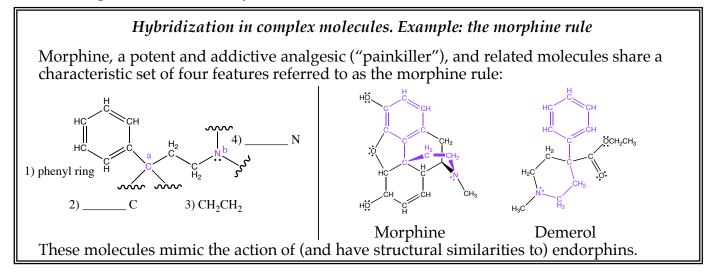
**Readings for today:** Section 7.1 – Spontaneous Change, Sections 7.2 and 7.8 – Entropy, Sections 7.12, 7.13, and 7.15 – Free Energy.

**Read for Lecture #18:** Section 7.16 – Free-Energy Changes in Biological Systems. (Assigned sections in chapter 7 are the same for the 3<sup>rd</sup> and the 4<sup>th</sup> ed.

Topics: Thermodynamics

 I. Enthalpies of reactions: calculating ΔH<sub>r</sub>° (continued from Lecture #16)
 II. Spontaneous change and free energy
 III. Entropy
 IV. Free energy of formation

Clicker question: review of hybridization



# **I. ENTHALPIES OF CHEMICAL REACTIONS** (continued from Lecture #16) **USING HESS'S LAW TO CALCULATE** ΔH<sub>r</sub>

Enthalpy is a "STATE" FUNCTION, which means  $\Delta H$  is \_\_\_\_\_\_ of path.

Enthalpy  

$$\begin{array}{c}
6 C_{gr} + 6 H_2 + 3 O_2 + 6 O_2 \\
-\Delta H^\circ_f = +1260. \text{ kJ/mol} \\
\text{decomposition of glucose to its} \\
\text{elements}
\end{array}$$
formation of 6 CO<sub>2</sub>  

$$\Delta H^\circ_f = 6(-393.5) = -2,361 \\
6 CO_2 + 6H_2 + 3O_2 \\
\hline
\Delta H^\circ = -2816 \text{ kJ} \\
6 CO_2 + 6 H_2O$$
formation of 6 H<sub>2</sub>O  

$$\Delta H^\circ_f = 6(-285.8) = -1715$$

**Hess's Law**: If two or more chemical equations are added to give another chemical equation, corresponding \_\_\_\_\_\_ must be added.

 $\Delta H^{\circ}$  for glucose oxidation (all values in kJ):

$$\Delta H_{r}^{\circ}$$

$$C_{6}H_{12}O_{6} + 6O_{2} \longrightarrow 6C_{gr} + 6H_{2} + 3O_{2} + 6O_{2}$$

$$6\left[C_{gr} + O_{2} \longrightarrow CO_{2}\right]$$

$$6\left[H_{2} + 1/2O_{2} \longrightarrow H_{2}O\right]$$

$$\overline{C_{6}H_{12}O_{6} + 6O_{2}} \longrightarrow 6CO_{2} + 6H_{2}O \quad \Delta H^{\circ} =$$

We have covered 3 methods (so far) to calculate  $\Delta$ Hr°:

1) \_\_\_\_\_ enthalpies (
$$\Delta H \text{ or } \Delta H_B$$
)  
 $\Delta H_r^\circ = \Sigma \Delta H_B$ (\_\_\_\_\_) -  $\Sigma \Delta H_B$ (\_\_\_\_\_)

2) Standard enthalpies of formation (\_\_\_\_)  $\Delta H_r^{\circ} = \Sigma \Delta H_f^{\circ} (\____) - \Sigma \Delta H_f^{\circ} (\____)$ 

3) Hess's law

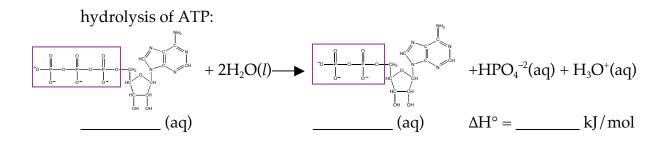
\*\*\* END OF EXAM #2 MATERIAL \*\*\*

# **II. SPONTANEOUS CHANGE AND FREE ENERGY**

A **spontaneous change** is a process that, given enough time, occurs without the need for outside intervention.

For example, the following reactions are spontaneous at constant pressure:

 $4Fe(s) + 3O_2(g) \rightarrow 2Fe_2O_3(s) \qquad \Delta H^\circ = \underline{\qquad } kJ/mol$  $H_3O^+(aq) + OH^-(aq) \rightarrow 2H_2O(l) \qquad \Delta H^\circ = \underline{\qquad } kJ/mol$ 



But so are these ...

 $H_2O(s) \rightarrow H_2O(l)$   $\Delta H^\circ = +6.95 \text{ kJ/mol}$ 

 $NH_4NO_3(s) \rightarrow NH_4^+(aq) + NO_3^-(aq)$ 

Is  $\Delta H$  the key to spontaneity? \_\_\_\_\_!

Condition for spontaneity under constant P + T involves GIBBS FREE ENERGY,  $\Delta G$ .

$\Delta G = \Delta H - T \Delta S$
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where T = temperature and  $\Delta$ S = change in entropy, a measure of disorder.

 $\Delta H^{\circ} = +28 \text{ kJ/mol}$ 

Under constant pressure and temperature, a process is spontaneous when  $\Delta G < 0$ , not necessarily when  $\Delta H < 0$ . Why?

 $\Delta G = \Delta H - T \Delta S$ Useful work or Amount of reaction FREE energy energy that gets "stuck"

Figuring this out was one of the towering achievements of thermodynamics!!

 $\Delta G^{\circ}$  is negative, even though  $\Delta H^{\circ}$  is positive. The reaction is **spontaneous**.

Now consider glucose oxidation at room temperature:

$$C_6H_{12}O_6 + 6O_2 \rightarrow 6CO_2 + 6H_2O$$
  
$$\Delta H^\circ = -2,816 \text{ kJ/mol}, \quad \Delta S^\circ = +233 \text{ J/K} \bullet \text{mol}$$

 $\Delta G^{\circ} = \underline{\qquad} - 298(\underline{\qquad}) = \underline{\qquad} kJ/mol$ 

 $\Delta G^{\circ}$  more negative than  $\Delta H^{\circ}$ . This reaction is spontaneous at \_\_\_\_\_\_ temperatures.

#### **III. ENTROPY**

Entropy, S, is a measure of the \_\_\_\_\_\_ of a system.  $\Delta S$  = change in entropy.  $\Delta S$  is a state function.

 $\Delta S^{\circ}$  positive  $\Rightarrow$  \_\_\_\_\_\_ in disorder

 $\Delta S^{\circ}$  negative  $\Rightarrow$  \_\_\_\_\_\_ in disorder

Disorder of gas \_\_\_\_\_ liquid \_\_\_\_\_ solid In solids, molecules cannot move around freely- they are locked in ordered locations.

Internal degrees of freedom – e.g. multiple molecular configurations, many quantum states that can be occupied - also contribute to entropy

Without calculations, we can predict the sign of  $\Delta S$  for many reactions. For example,

 $2H_2O_2(l) \rightarrow 2H_2O(l) + O_2(g)$  has a \_\_\_\_\_  $\Delta S$ .

# Entropy for reactions, $\Delta S_r^{\circ}$

can be calculated from absolute entropies of products and reactants,

 $\Delta S_r^{\circ} = \Sigma S^{\circ}(\underline{\qquad}) - \Sigma S^{\circ}(\underline{\qquad})$ 

where S° is the absolute standard entropy.

Unlike E or H, where the zero can be selected, S has an absolute zero – the perfect crystal at T = 0 K (perfectly ordered, no disorder at all).

For example, consider the decomposition of hydrogen peroxide.

$$2H_2O_2(l) \rightarrow 2H_2O(l) + O_2(g)$$
  

$$\Delta S_r^{\circ} = \Sigma S^{\circ}(\text{products}) - \Sigma S^{\circ}(\text{reactants})$$
  

$$\Delta S^{\circ} = \underline{S^{\circ}(\underline{\phantom{S}}) + S^{\circ}(\underline{\phantom{S}}) - \underline{S^{\circ}(\underline{\phantom{S}})}$$
  

$$\Delta S^{\circ} = 2(70. \text{ JK}^{-1}\text{mol}^{-1}) + (205 \text{ JK}^{-1}\text{mol}^{-1}) - 2(110. \text{ JK}^{-1}\text{mol}^{-1})$$
  

$$\Delta S^{\circ} = \underline{J}K^{-1}\text{mol}^{-1}$$

Why is  $\Delta S^{\circ}$  positive? The reaction converts liquid  $\rightarrow$  liquid and gas.

 $\begin{array}{l} \Delta G^{\circ} &= \Delta H^{\circ} - T \Delta S^{\circ} \\ &= -196 \ kJ/mol - 298.15 \ K \ (\_\_\_\_ kJ \ K^{-1}mol^{-1}) \\ &= -233 \ kJ/mol \qquad (The reaction is \_\_\_\_) \end{array}$ 

Now consider ice melting at 298.15 K.  $H_2O(s) \rightarrow H_2O(l)$ 

 $\Delta S^{\circ} = S^{\circ}(\_\_\_) - S^{\circ}(\_\_\_) = 69.91 - 41.32$   $\Delta S^{\circ} = 28.59 \text{ J K}^{-1} \text{ mol}^{-1}$ Why is  $\Delta S^{\circ} > 0$ ?

 $\Delta G^{\circ} = 6.95 - 298.15 \text{K}(2.859 \text{ x } 10^{-2} \text{ kJ/K mol})$ = -1.57 kJ/mol Ice melting is spontaneous at room temperature even though  $\Delta H^{\circ}$  is positive.

#### IV. FREEE ENERGY OF FORMATION, $\Delta G_f$

analogous to  $\Delta H_{f}$ 

 $\Delta G_{f}^{o}$  = standard Gibbs free energy of formation

=  $\Delta G_r^{o}$  for formation of 1 mol of compound from its elements in their most stable form in the standard states at P = 1 bar and T = 298.15 K.

Tabulated for many compounds like  $\Delta H_{f}^{o}$ , but can also be calculated from

 $\_\_\_ - T\Delta S^{\circ}$ 

For example,

 $C(gr) + O_2(g) \rightarrow CO_2(g) \qquad \qquad \Delta G^\circ = -394.36 \text{ kJ/mol} = \Delta G_f^\circ$ 

 $\Delta G_{f}^{o}$  is important because it is a measure of a compound's stability relative to its elements.

If  $\Delta G_f^{\circ} < 0$ , a compound is thermodynamically \_\_\_\_\_\_ relative to its elements. If  $\Delta G_f^{\circ} > 0$ , a compound is thermodynamically \_\_\_\_\_\_ relative to its elements.

 $\begin{array}{ll} 6C(gr) + 3H_2(g) \rightarrow C_6H_6(l) & \Delta G_f^{\,o} = 124 \ kJ/mol \\ C_6H_6(l) \rightarrow 6C(gr) + 3H_2(g) & \Delta G^o = -124 \ kJ/mol \end{array}$ 

The reverse reaction is spontaneous, but very, very slow!

Free energy tells whether or not a reaction will happen spontaneously, but it tells us \_\_\_\_\_\_\_ about the rate of the reaction (for rate information we need chemical kinetics).

To calculate  $\Delta G^{\circ}$  for a reaction...

 $\Delta G_r^{\circ} = \Sigma \Delta G_f^{\circ}(\text{products}) - \Sigma \Delta G_f^{\circ}(\text{reactants})$ 

OR  $\Delta G_r^{\circ} = \Delta H_r^{\circ} - T\Delta S_r^{\circ}$ 

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