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$$\left(\frac{\dot{a}}{a}\right)^2 = \left(\frac{\dot{x}}{x}\right)^2 = \frac{H_0^2}{x^4} \left(\Omega_{m,0}x + \Omega_{\mathrm{rad},0} + \Omega_{\mathrm{vac},0}x^4 + \Omega_{k,0}x^2\right) \ .$$

$$\Omega_{k,0} = 1 - \Omega_{m,0} - \Omega_{\mathrm{rad},0} - \Omega_{\mathrm{vac},0} \; .$$

Finally,

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$$t_0 = \frac{1}{H_0} \int_0^1 \frac{x dx}{\sqrt{\Omega_{m,0} x + \Omega_{\rm rad,0} + \Omega_{\rm vac,0} x^4 + \Omega_{k,0} x^2}} \,.$$

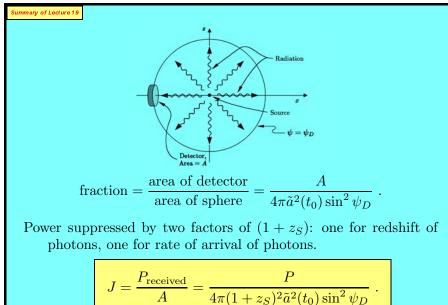
Closed Universe:

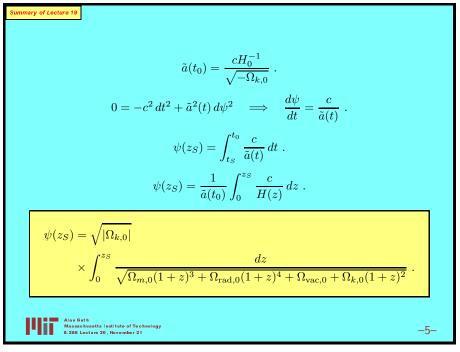
$$ds^{2} = -c^{2} dt^{2} + \tilde{a}^{2}(t) \left\{ d\psi^{2} + \sin^{2} \psi \left( d\theta^{2} + \sin^{2} \theta \, d\phi^{2} \right) \right\} ,$$

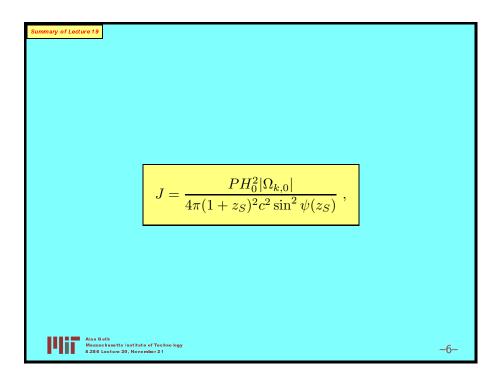
where  $\sin \psi \equiv \sqrt{k} r$ .

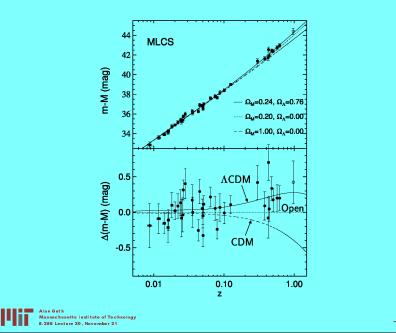
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