

Euclid's Postulates



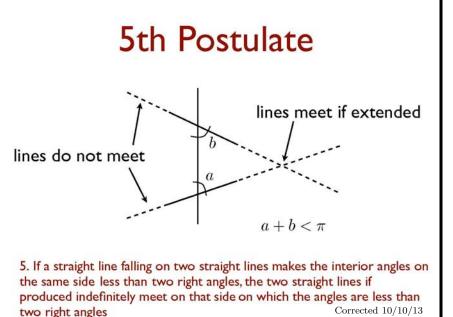
- 1. A straight line segment can be drawn joining any two points.
- 2. Any straight line segment can be extended indefinitely in a straight line.
- 3. Given a straight line segment, a circle can be drawn having the segment as radius and one endpoint as center.

4. All right angles are congruent.

5. If a straight line falling on two straight lines makes the interior angles on the same side less than two right angles, the two straight lines if produced indefinitely meet on that side on which the angles are less than two right angles

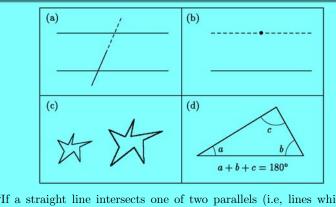
Corrected 10/10/13

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Equivalent Statements of the 5th Postulate



(a) "If a straight line intersects one of two parallels (i.e, lines which do not intersect however far they are extended), it will intersect the other also."

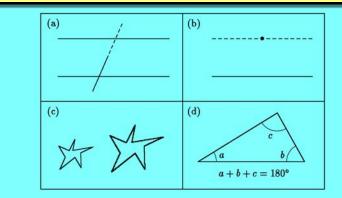
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(b) "There is one and only one line that passes through any given point and is parallel to a given line."

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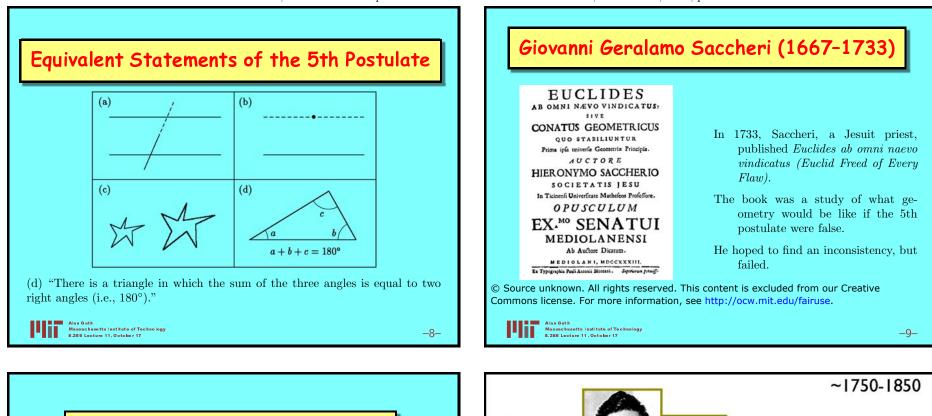
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Equivalent Statements of the 5th Postulate



(c) "Given any figure there exists a figure, similar to it, of any size." (Two polygons are similar if their corresponding angles are equal, and their corresponding sides are proportional.)

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Carl Friedrich Gauss (1777-1855)



German mathematician and physicist.

- Born as the son of a poor working-class parents. His mother was illiterate and never even recorded the date of his birth.
- His students included Richard Dedekind, Bernhard Riemann, Peter Gustav Lejeune Dirichlet, Gustav Kirchhoff, and August Ferinand Möbius.

Photo from http://commons.wikimedia.org/wiki/File: Carl_Friedrich_Gauss.jpg (in public domain).



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Gauss 5th Postulate $a+b+c<\pi!$ Slides courtesy of Mustafa Amin. Used with permission.

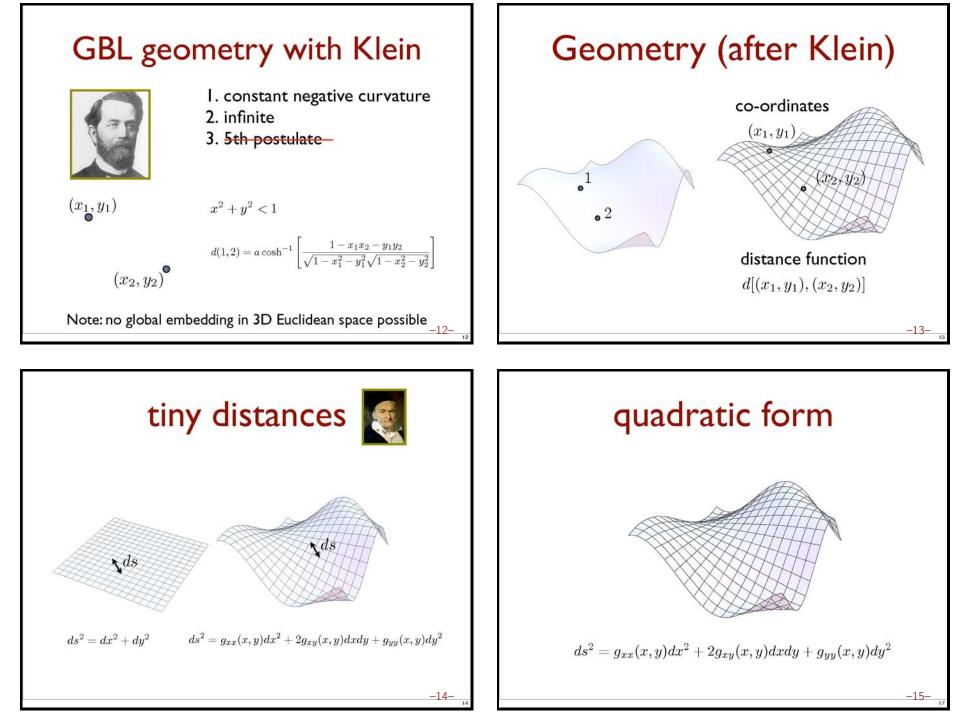
Lobachevski

Bolyai

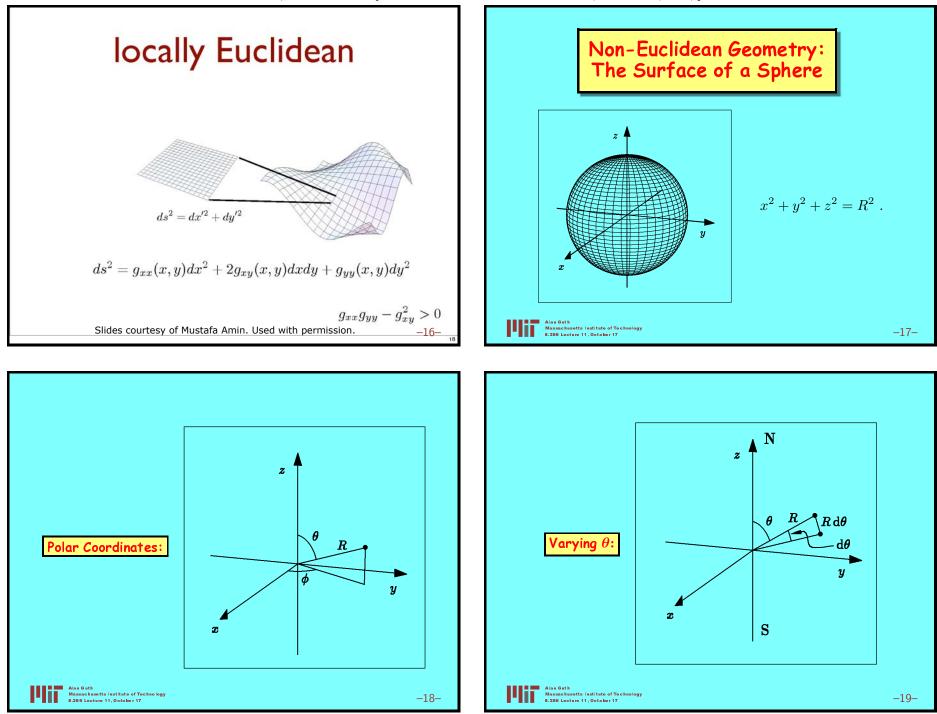
infinite

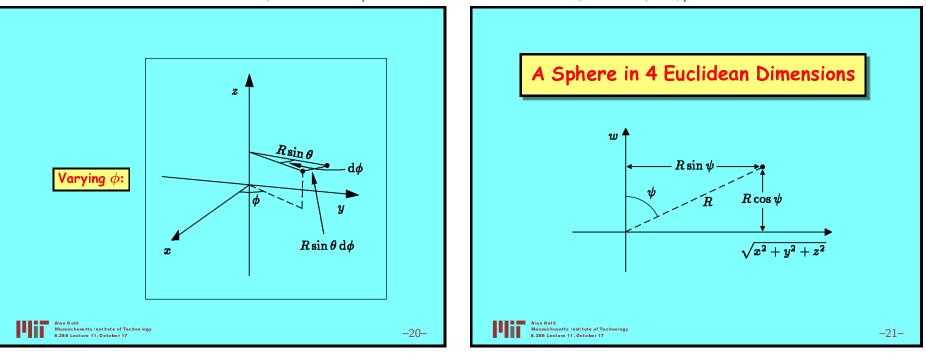
constant negative curvature

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Alan Guth, Non-Euclidean Spaces: Closed Universes 8.286 Lecture 11, October 17, 2013, p. 6.

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