

Now that we've calculated the change in potential energy between some initial and final heights for the gravitational problem, mg of y final minus y initial.

For this conservative force of gravity, and we had our coordinate system like that, we were able to calculate the change in potential energy.

And remember our theorem is that non-conservative work equals ΔK plus ΔU .

Now what we'd like to do is establish the concept of a reference point for potential energy.

And we'll do that as follows, see the change in potential energy only depended on say, our initial state and our final state.

What we'd like to do is introduce the concept of a reference point.

So let's identify some point Y_p to be our reference point.

And we'll define a potential U_p to be the reference potential.

And if we want to talk about the potential energy in a final state, we'll always refer it to the difference between that and the reference point.

So this is ΔU between the final state and the reference point.

Likewise, for the initial state, we'll always refer that with respect to our reference point.

So any state that we have, we can always refer the potential energy difference between some state and some reference point.

Why do we do this?

Because notice that if we look at U_{final} minus $U_{\text{reference point}}$, and we subtract from that U_{initial} minus $U_{\text{reference point}}$, then the difference-- the reference points here we have a minus, here we have a plus-- this is just equal to U_{final} minus U_{initial} , which is ΔU .

So the change in potential energy between any two states is independent of how we choose our reference potential.

But it can make calculations easier when we can identify what the potential energy is for a little state.

Now let's look at our example.

So for our gravitational problem we will choose y reference point to be 0.

And we'll choose the potential energy at this reference point also to be 0.

So our reference potential at the origin is 0, and I'll denote it like that.

Then the potential energy at some initial state minus the reference point-- well, we can use our formula here, because this is between any two states.

So this is $mg y_{\text{initial}}$ minus the reference point.

But our reference point was 0, and so we see that U_{initial} minus $y_{\text{reference}}$ point, which was also 0, is just equal to $mg Y_i$.

And so we have this statement that the potential energy difference between our initial state and the reference point is just mg where Y_i is the height that the initial state is above the reference point.

In a similar way, we have U_{final} is $mg y_{\text{final}}$.

And so we see we recover what we expect.

This is just $mg y_{\text{final}}$ minus y_{initial} .

Now this we can generalize just a little bit by saying that for any-- let's write that for us our mass, which is for any height y our potential energy function for the gravitational force $U(y)$ is equal to $mg y$.

That's a formula that many of you have seen before.

But it's very important to note that with this formula, U of 0 equals 0, because that's our reference point.

And that becomes our potential energy function for the gravitational force.

Now our next step will be to do the same thing for spring forces and inverse square gravitational forces.

And we'll also look at graphical analysis of this function.