2.081J/16.230J Plates and Shells

Homework #1 Due date: Class on Tuesday February 21

PROBLEM 1

Consider a square plate subjected to a certain type of loading. Under this loading, the plate assumes a shape of a paraboloid:

$$w = -\frac{M}{2D\left(1+\nu\right)}\left(x^2 + y^2\right)$$

where M is the applied edge moment, D is the bending rigidity of the plate, and ν is the Poisson ratio.



Determine:

- 1. (a) components of the curvature tensor, $\kappa_{\alpha\beta}$
 - (b) components of the bending moment tensor, $M_{\alpha\beta}$
 - (c) shear force vector, Q_{α}
 - (d) bending moments and shear forces on all four edges
 - (e) corner forces

PROBLEM 2

Consider the "anticlastic" deflection profile of the plate given by:



 $w = -\frac{M}{2D\left(1-\nu\right)} \left(x^2 - y^2\right)$

Answer the questions (a) through (e) of the Problem 1.

PROBLEM 3

Derive equations of equilibrium of the plate from the free body diagram, shown below:

