# 18.335 Fall 2008 <br> Performance Experiments with Matrix Multiplication 

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Hardware: 2.66 GHz Intel Core 2 Duo
64-bit mode, double precision, gcc 4.1.2
optimized BLAS dgemm: ATLAS 3.6.0
http://math-atlas.sourceforge.net/

## A trivial problem? <br> $$
\underset{m \times p}{C}=\underset{m \times n}{A} \underset{n \times p}{B}
$$

the "obvious" C code:

```
/* C = A B, where A is m x n, B is n x p,
    and C is m x p, in row-major order */
void matmul(const double *A, const double *B,
    double *C, int m, int n, int p)
{
    int i, j, k;
    for (i = 0; i < m; ++i)
    for (j = 0; j < p; ++j) {
            double sum = 0;
            for (k = 0; k < n; ++k)
                    sum += A[i*n + k] * B[k*p + j];
            C[i*p + j] = sum;
    }
}
```

for $i=1$ to $m$
for $j=1$ to $p$ $C_{i j}=\sum_{k=1}^{n} A_{i k} B_{k j}$
$2 m n p$ flops
(adds+mults)
just three loops, how complicated can it get?

## flops/time is not constant! <br> (square matrices, $m=n=p$ )



## Not all "noise" is random



## All flops are not created equal



## Things to remember

- We cannot understand performance without understanding memory efficiency (caches).
- ~10 times more important than arithmetic count
- Computers are more complicated than you think.
- Even a trivial algorithm is nontrivial to implement well.
- matrix multiplication: 10 lines of code $\rightarrow 130,000+$ (ATLAS)

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