## Exercises on transposes, permutations, spaces

Problem 5.1: (2.7 \#13. Introduction to Linear Algebra: Strang)
a) Find a 3 by 3 permutation matrix with $P^{3}=I$ (but not $P=I$ ).
b) Find a 4 by 4 permutation $\widehat{P}$ with $\widehat{P}^{4} \neq I$.

Problem 5.2: Suppose $A$ is a four by four matrix. How many entries of $A$ can be chosen independently if:
a) $A$ is symmetric?
b) $A$ is skew-symmetric? $\left(A^{T}=-A\right)$

Problem 5.3: (3.1 \#18.) True or false (check addition or give a counterexample):
a) The symmetric matrices in $M$ (with $A^{T}=A$ ) form a subspace.
b) The skew-symmetric matrices in $M$ (with $A^{T}=-A$ ) form a subspace.
c) The unsymmetric matrices in $M$ (with $A^{T} \neq A$ ) form a subspace.

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