Exercises on transposes, permutations, spaces

Problem 5.1: (2.7 #13. Introduction to Linear Algebra: Strang)

- a) Find a 3 by 3 permutation matrix with $P^3 = I$ (but not P = I).
- b) Find a 4 by 4 permutation \widehat{P} with $\widehat{P}^4 \neq I$.

Problem 5.2: Suppose *A* is a four by four matrix. How many entries of *A* can be chosen independently if:

- a) *A* is symmetric?
- b) A is skew-symmetric? $(A^T = -A)$

Problem 5.3: (3.1 #18.) True or false (check addition or give a counterexample):

- a) The symmetric matrices in *M* (with $A^T = A$) form a subspace.
- b) The skew-symmetric matrices in *M* (with $A^T = -A$) form a subspace.
- c) The unsymmetric matrices in *M* (with $A^T \neq A$) form a subspace.

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