Geometric definition of the derivative:

We're still trying to find a computational method of finding the equation of the tangent line - how do we compute the value of m?

In general, how do we know which lines are tangent lines and which lines are not?



Figure 1: A graph with secant and tangent lines

A secant line is a line that joins two points on a curve. If the two points are close enough together, the slope of the secant line is close to the slope of the curve. We want to find the slope of the tangent line m — which equals the slope of the curve — and we use the slopes of secant lines to do this.

Suppose PQ is a secant line of the graph of f(x). We can find the slope of the graph at P by calculating the slope of PQ as Q moves closer and closer to P (and the slope of PQ gets closer and closer to m).

The tangent line equals the limit of secant lines PQ as $Q \to P$; here P is fixed and Q varies.

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