

LECTURE 2 : THE FORCE TRANSDUCER

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Objectives: To understand the basic principles of how high resolution force transducers function, their physical limitations, and applications.

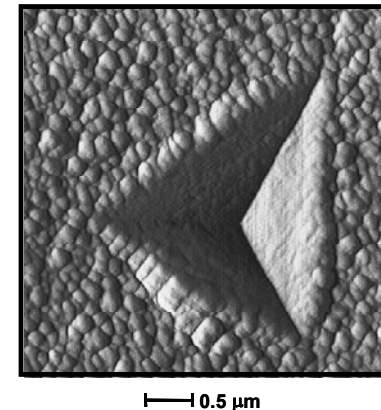
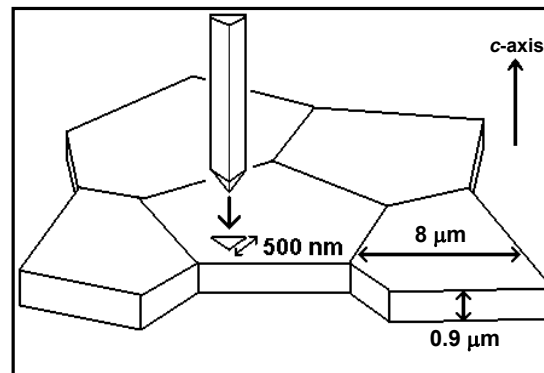
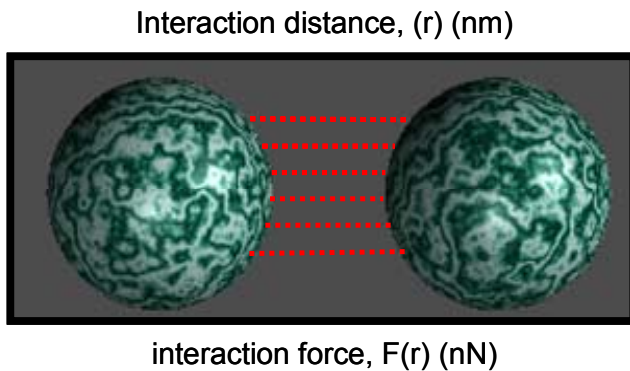
Readings: Course Reader Documents 6-8

The study of forces, motions, energies, and deformations : much of 3.032 was *continuum mechanics*

LAST TIME : WHAT IS NANOMECHANICS? → subset of the field of nanotechnology, involving nN-scale forces or nm-scale displacements (nano= $1 \bullet 10^{-9}$)

1. Noncontact : High Resolution Force Spectroscopy, surface forces measurement (e.g. electrostatics, van der Waals forces, etc.)

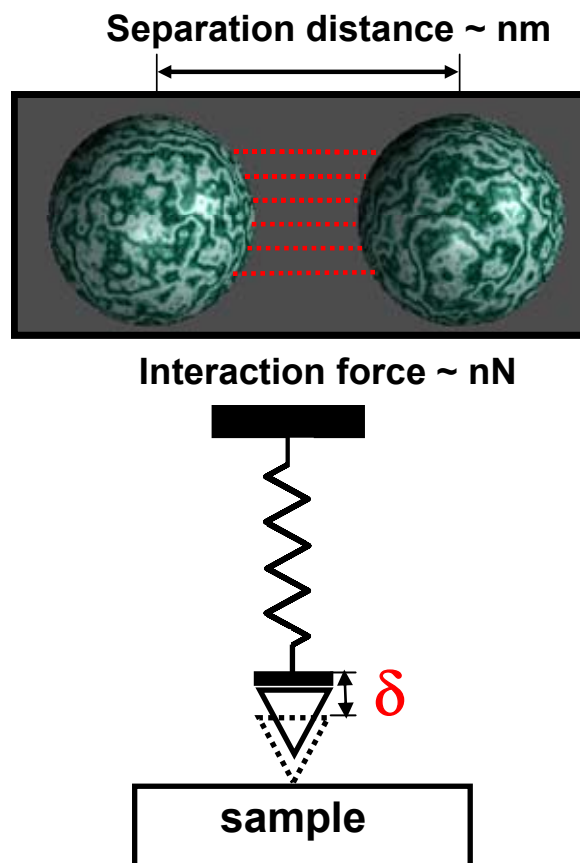
2. Contact : Nanoindentation, single cell tensile testing (e.g. elasticity, plasticity, → dislocations) etc.



Courtesy of Benjamin Bruet and Journal of Materials Research. Used with permission.

HOW CAN WE MEASURE SUCH TINY FORCES?

i.e. nN ($=1 \cdot 10^{-9}$ N), even pN ($=1 \cdot 10^{-12}$ N) ! \rightarrow typical engineering structures are Newtons



Force Transducer - sensor device that responds to an external force where you can output and record that response

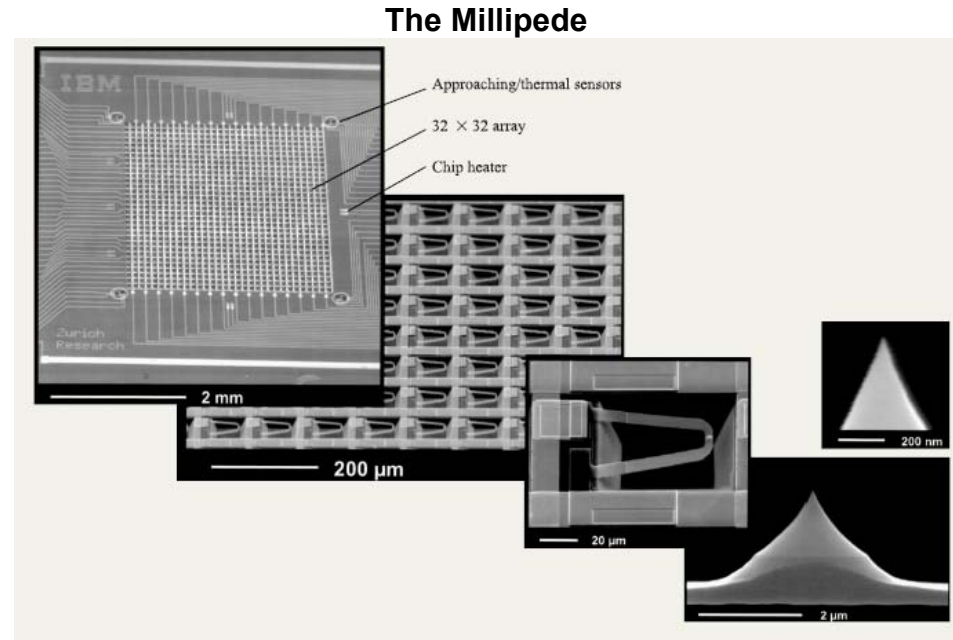
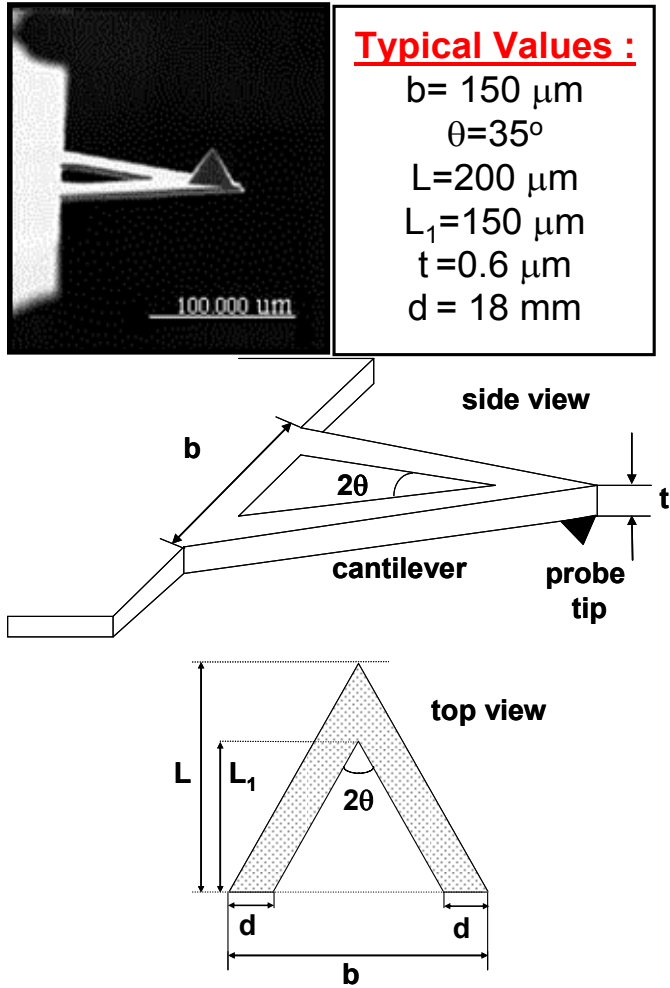
Transducer Calibration - determine the relationship between the externally applied force and output signal to automatically convert to a force

1) high sensitivity and 2) small in dimensions, fine probe (\sim nm)

- Typically a **spring** (not conventional!) which deflects in response to an external force, δ = transducer (spring displacement), know the elastic properties (stiffness) of the spring (i.e. Hooke's Law) you can convert into force, F .

$$F = k\delta$$

EXAMPLE OF A FORCE TRANSDUCER- Microfabricated Cantilever Beams With Nanosized Probe Tips



Vettiger, et al. *IBM J. Res. Develop.* 44 3 2000 323

Courtesy of IBM. Used with permission.

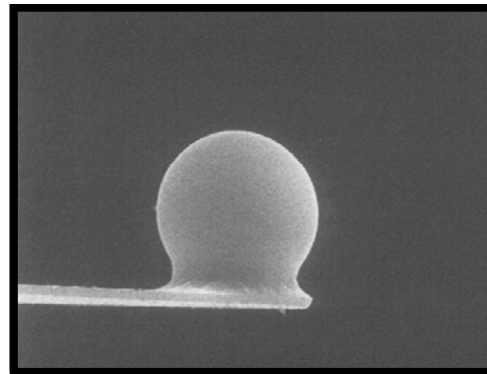
Potential Applications :

- 1) thermomechanical data storage in thin polymer media - High throughput
- 2) imaging/characterization
- 3) nanolithography
- 4) atomic and molecule manipulations

ATTACHMENTS TO NANOSIZED PROBES AT THE END OF MICROFABRICATED CANTILEVERS

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Single Cell *Dictyostelium Discoideum*
(Benoit, et al. *Nature Cell. Bio* **2000**, 2 (6), 313.)



Colloid : Seog, Ortiz/ Grodzinsky Labs 2001

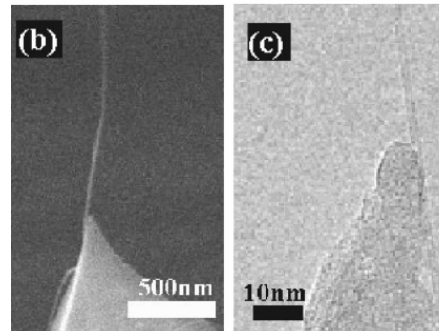
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Nanotube Tips (Biomolecule Functionalized) :
Wong et al. *Nature* **1998**, 394 (6688), 52.

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E. Coli Bacteria Ong, et al. *Langmuir* **1999**, 15, 2719.

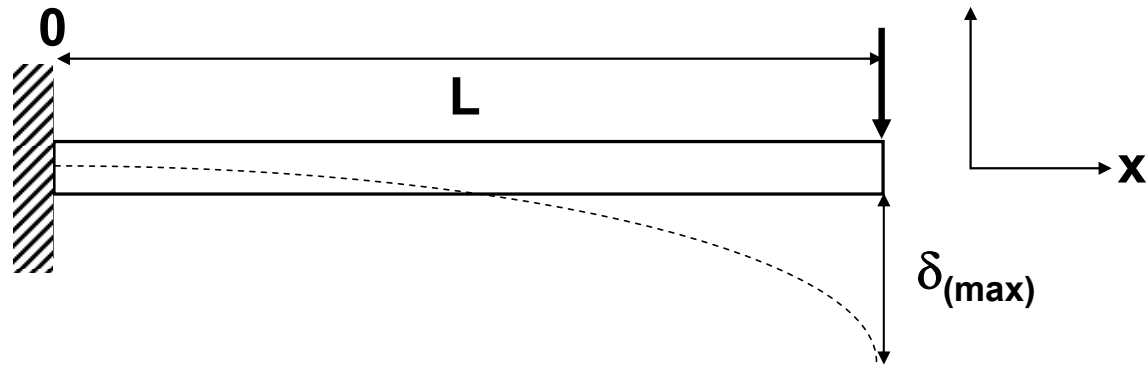
Nanotube Tips :



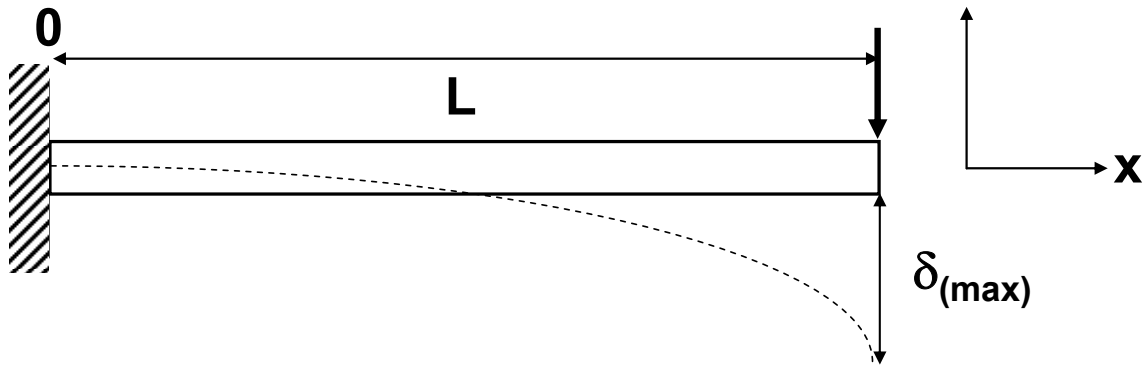
Courtesy of American Institute of Physics. Used with permission.

Fig. 2b and c in Yenilmez, E. et al. "Wafer scale production of carbon nanotube scanning probe tips for atomic force microscopy." *Applied Phys Lett* 80, no. 12 (2002): 2225.

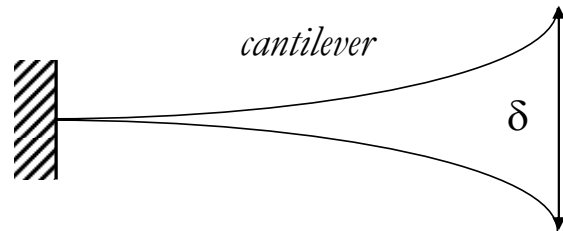
CANTILEVER BEAM THEORY



CANTILEVER BEAM THEORY (CONT'D)



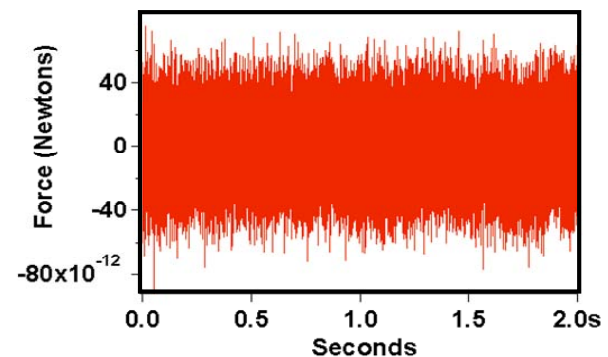
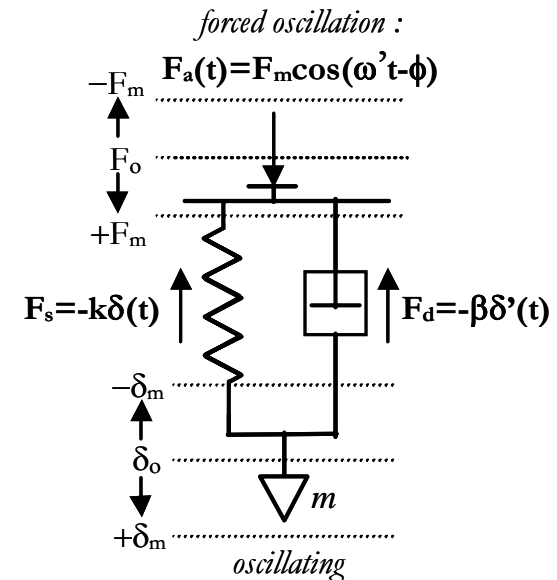
LIMIT OF FORCE DETECTION : THERMAL OSCILLATIONS



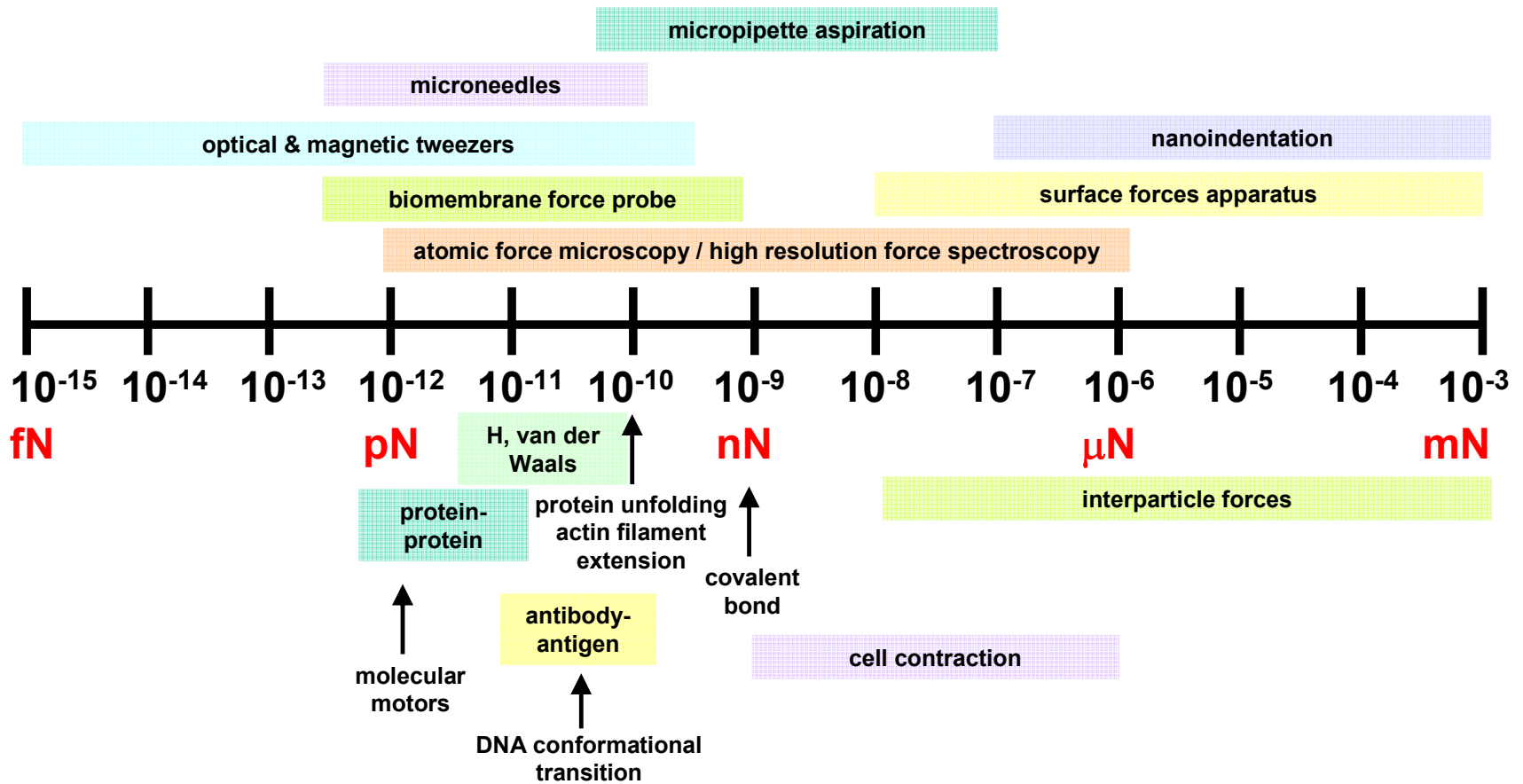
In the absence of any externally applied forces [e.g. far away from the cantilever surface], a high resolution force transducer will oscillate at its natural resonant frequency (maximum displacement of the amplitude of the oscillations) due to a non-zero thermal energy, $k_B T$ (room temperature) = $4.1 \cdot 10^{-21}$ J \rightarrow **the system can be modeled as a driven, damped harmonic oscillator.**

These oscillations are the background noise in the nanomechanical experiment and are given by the following equation :

$$F_{min} = 1.007t \left(\frac{w}{lQ} \right)^{1/2} (E\rho)^{1/4} (k_B T b)^{1/2}$$



FORCE RANGE FOR VARIOUS NANOMECHANICAL INSTRUMENTS



BIOSENSORS

Podcast: Lipid Bilayer Formation

Guest: Professor **Jurgen Fritz** (International University Bremen; soon to be Jacobs University Bremen, Germany)

Citation : Pera, I. & Fritz, J. Sensing lipid bilayer formation and expansion with a microfabricated cantilever array. *Langmuir*. 23, 1543-1547 (**2007**)