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 Fundamental Thm. of Arithmetic Every integer > 1factors uniquely into a weakly decreasing sequence of primes 0000 Albert R Meyer March 5, 2012 lec 5M.10

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Prime Divisibility Lemma: p prime and p | ab implies pla or plb pf: say not(p|a), so gcd(p,a) = 1tpb = 1 b sab + S0, p p so pl QED @09 Albert R Meyer March 5, 2012 lec 5M.12



Unique Prime Factorization pf: suppose not. choose smallest n > 1: $n = p_1 \cdot p_2 \cdots p_k = q_1 \cdot q_2 \cdots q_m$ $p_1 \ge p_2 \ge \cdots \ge p_k$ $q_1 \ge q_2 \ge \cdots \ge q_m$ If $q_1 = p_1$, then $p_2 \cdots p_k = q_2 \cdots q_m$ is smaller nonunique.

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 Unique Prime Factorization Every integer n > 1 has a unique factorization into primes: $\mathbf{p}_1 \cdots \mathbf{p}_k = \mathbf{n}$ with $\mathbf{p}_1 \geq \mathbf{p}_2 \geq \cdots \geq \mathbf{p}_k$ $\bigcirc 0 0 0 0$ Albert R Meye March 5, 2012 lec 5M 14





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