12.842 / 12.301 Past and Present Climate Fall 2008

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Radiative Transfer Chapter 3, Hartmann

- Shortwave Absorption:
  Clouds, H<sub>2</sub>0, O<sub>3</sub>, some CO<sub>2</sub>
- Shortwave Reflection:
  Clouds, surface, atmosphere
- Longwave Absorption:
  Clouds, H<sub>2</sub>0, CO<sub>2</sub>, CH<sub>4</sub>, N<sub>2</sub>O

### Planck's Law

- Based on assumption of local thermodynamic equilibrium
  - (Not valid at very high altitudes in atmosphere)

$$B_{\upsilon}(T) = \frac{2\hbar\upsilon^3}{c^2 \left[ e^{\frac{\hbar\upsilon}{kT}} - 1 \right]}$$

- k = Boltzmann's constant
- $\hbar = Planck's constant$
- v = frequencyc = speed of light

Stefan-Boltzmann Law is the integral of the Planck function over all frequencies and all angles in a hemisphere:

$$\pi \int_0^\infty B_v(T) d\upsilon = \sigma T^4$$
$$\sigma = \frac{2\pi^5 k^4}{15c^2 \hbar^3}$$

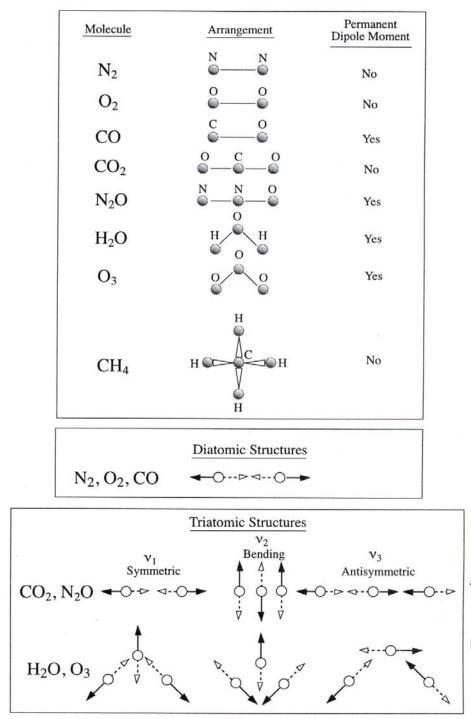
# Absorption and Emission in a Gas:

Photon energy  $E_{\upsilon} = \hbar \upsilon$ 

Atomic energy levels  $E_{\nu} = n\hbar\nu, n = 0, 1, 2, 3...$ 

An isolated atom can absorb only those photons whose energy is equal to the difference between two atomic energy levels

Molecules have additional energy levels:



These images are copyrighted by Academic Press, NY, 1999. The images are in a chapter entitled "Quasi-equilibrium thinking" (author is Kerry Emanuel) that appears in the book entitled "General circulation model development: past, present and future", edited by D. Randall, Ed. ISBN: 0125780109. Used with permission. For molecules in a gas:

$$E_{total} = E_{atomic} + E_{vibrational} + E_{rotational} + E_{translational}$$

Translational energy is the kinetic energy of molecular motions in a gas, proportional to the gas temperature. Not quantized.

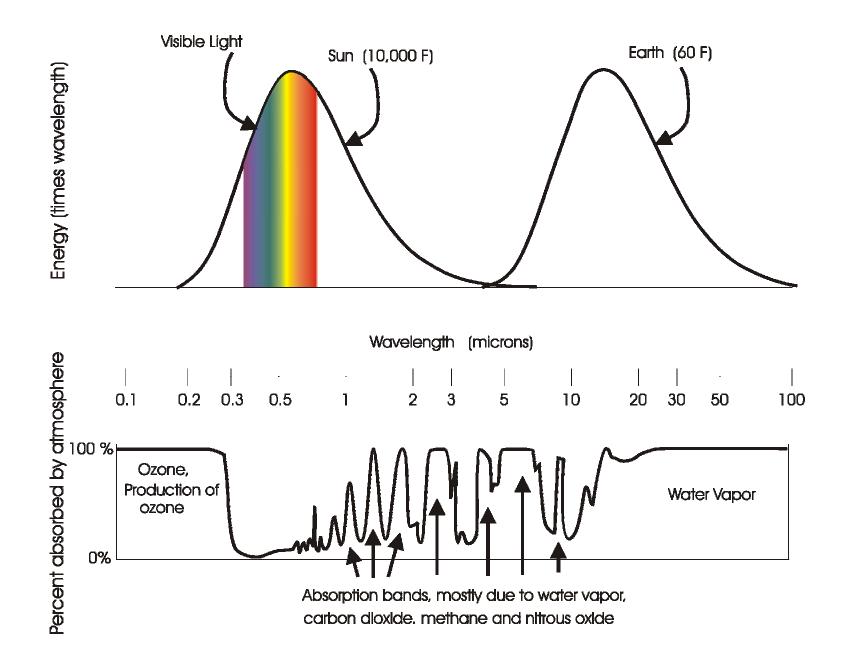
Molecules in a gas can absorb more frequencies than isolated atoms.

Collisions between molecules can carry away energy or supply energy to interactions between matter and photons.

Natural, pressure and Doppler broadening

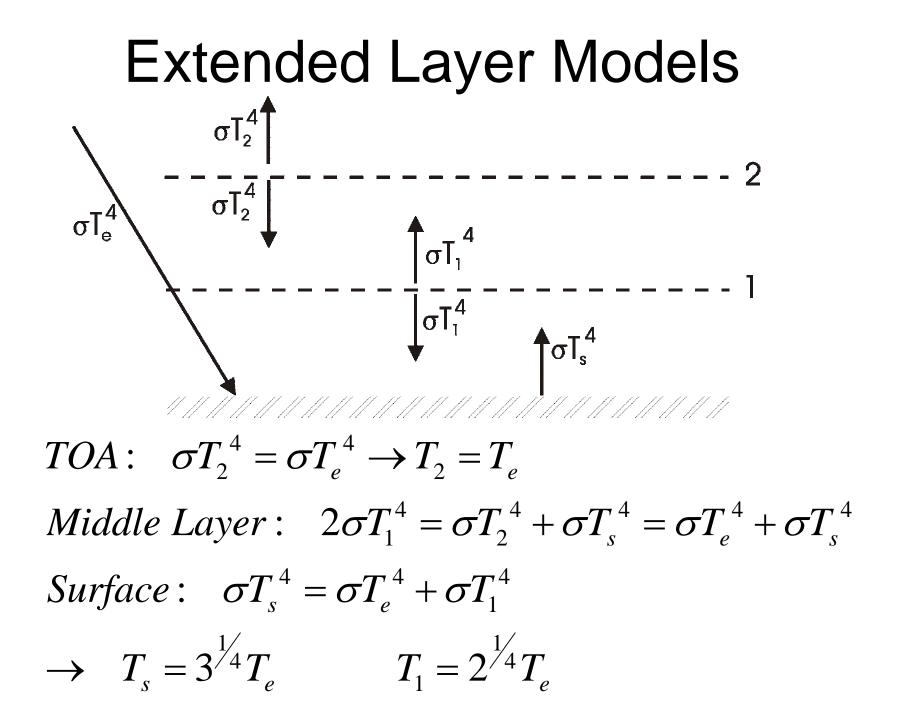
### Principal Atmospheric Absorbers

- H<sub>2</sub>O: Bent triatomic, with permanent dipole moment and pure rotational bands as well as rotation-vibration transitions
- O<sub>3</sub>: Like water, but also involved in photodissociation
- CO<sub>2</sub>: No permanent dipole moment, so no pure rotational transitions, but temporary dipole during vibrational transitions
- Other gases: N<sub>2</sub>O, CH<sub>4</sub>

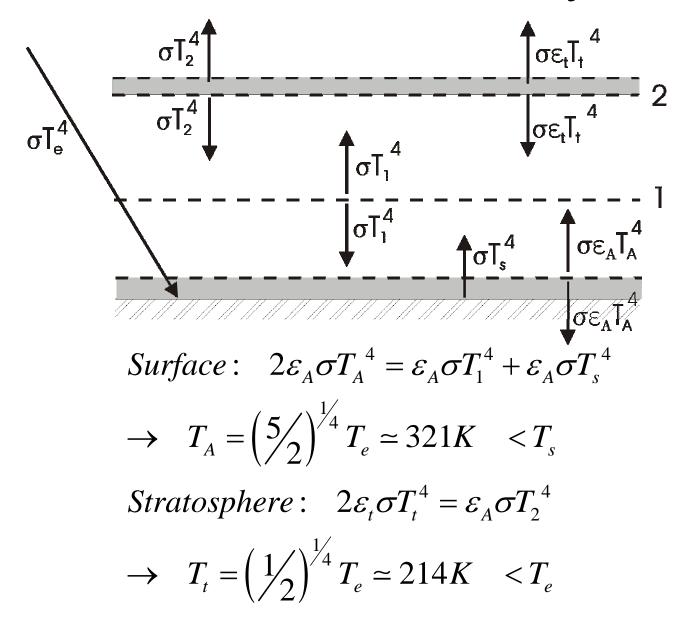


### **Radiative Equilibrium**

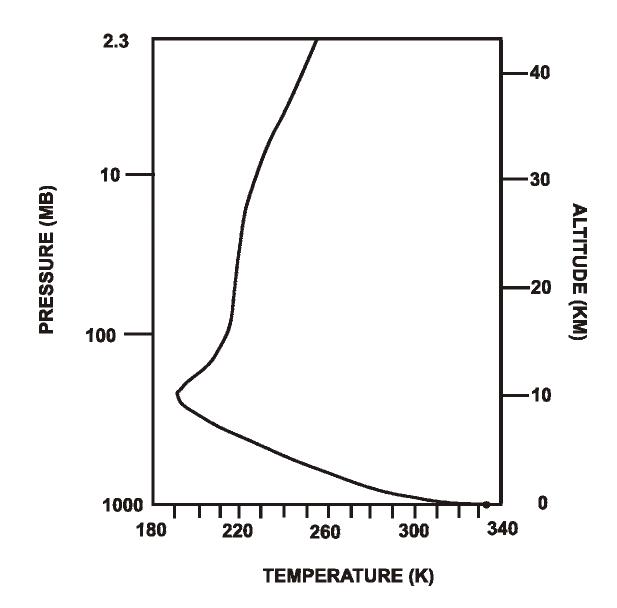
- Equilibrium state of atmosphere and surface in the absence of non-radiative enthalpy fluxes
- Radiative heating drives actual state toward state of radiative equilibrium



#### Effects of emissivity<1



Full calculation of radiative equilibrium:



Problems with radiative equilibrium solution:

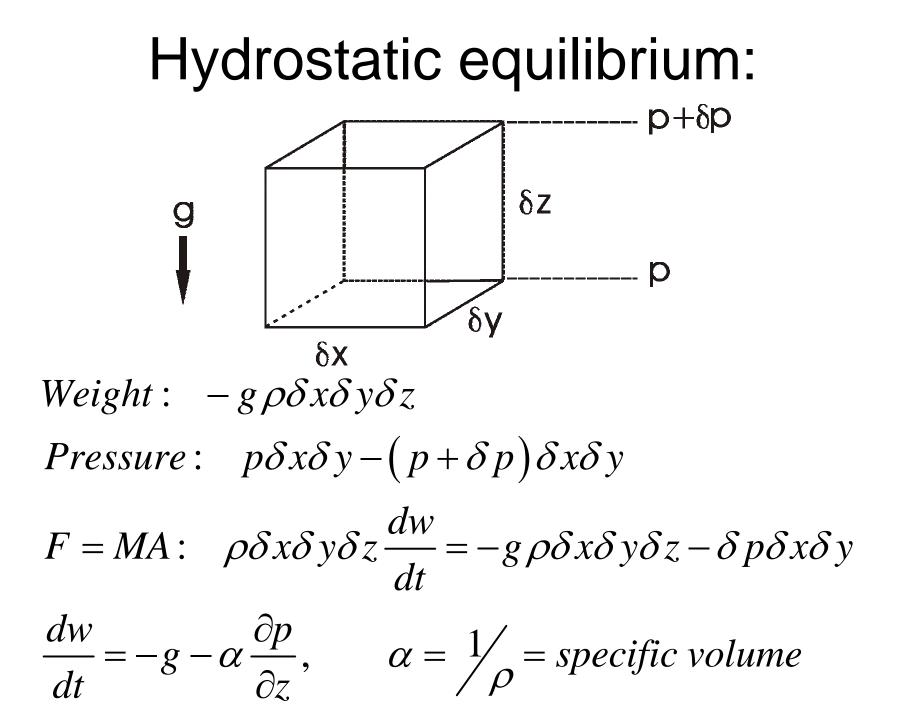
- Too hot at and near surface
- Too cold at a near tropopause
- Lapse rate of temperature too large in the troposphere
- (But stratosphere temperature close to observed)

### Missing ingredient: Convection

- As important as radiation in transporting enthalpy in the vertical
- Also controls distribution of water vapor and clouds, the two most important constituents in radiative transfer

# When is a fluid unstable to convection?

- Pressure and hydrostatic equilibrium
- Buoyancy
- Stability

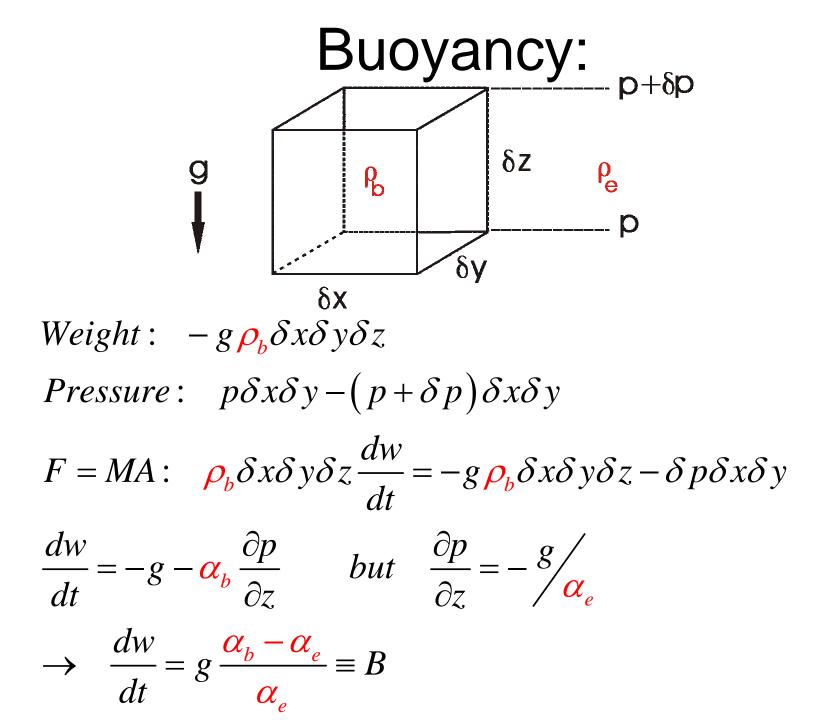


# Pressure distribution in atmosphere at rest:

Ideal gas: 
$$\alpha = \frac{RT}{p}, \qquad R \equiv \frac{R^*}{\overline{m}}$$
  
Hydrostatic:  $\frac{1}{p} \frac{\partial p}{\partial z} = -\frac{g}{RT}$ 

Isothermal case:  $p = p_0 e^{-z/H}$ ,  $H \equiv \frac{RT}{g} = "scale height"$ 

Earth: H~ 8 Km



### **Buoyancy and Entropy**

Specific Volume:

 $\alpha = \frac{1}{\rho}$ 

Specific Entropy: s

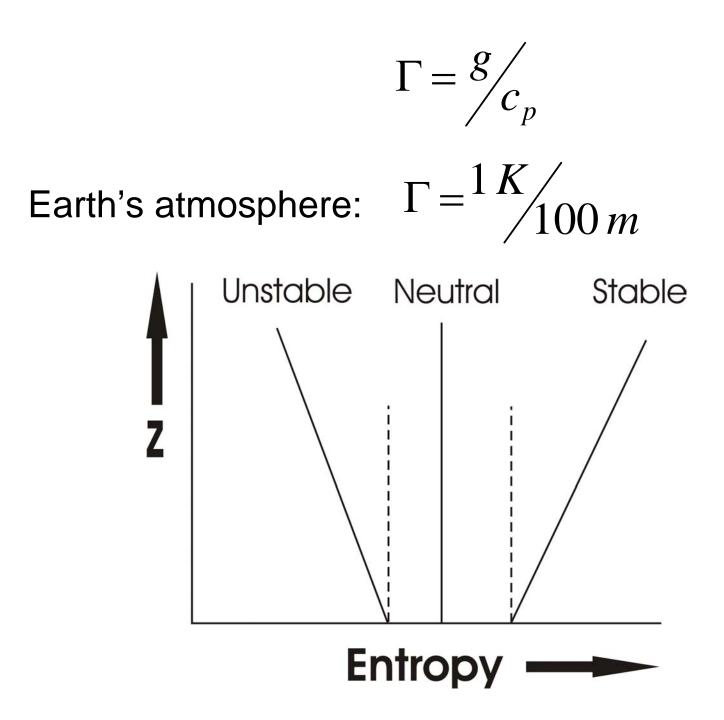
 $\alpha = \alpha(p, s)$ 

$$\left(\delta\alpha\right)_{p} = \left(\frac{\partial\alpha}{\partial s}\right)_{p} \delta s = \left(\frac{\partial T}{\partial p}\right)_{s} \delta s$$
$$B = g \frac{\left(\delta\alpha\right)_{p}}{\alpha} = \frac{g}{\alpha} \left(\frac{\partial T}{\partial p}\right)_{s} \delta s = -\left(\frac{\partial T}{\partial z}\right)_{s} \delta s \equiv \Gamma \delta s$$

#### The adiabatic lapse rate:

First Law of Thermodynamics :

 $\dot{Q} = T \frac{ds_{rev}}{dt} = c_v \frac{dT}{dt} + p \frac{d\alpha}{dt}$  $=c_{v}\frac{dT}{dt} + \frac{d\left(\alpha p\right)}{dt} - \alpha \frac{dp}{dt}$  $=(c_v+R)\frac{dT}{dt}-\alpha\frac{dp}{dt}$  $=c_p \frac{dT}{dt} - \alpha \frac{dp}{dt}$ Adiabatic:  $c_n dT - \alpha dp = 0$ *Hydrostatic* :  $c_n dT + g dz = 0$  $\rightarrow \left(\frac{dT}{dz}\right)_{s} = -\frac{g}{c_{n}} \equiv -\Gamma_{d}$ 



### Model Aircraft Measurements (Renno and Williams, 1995)

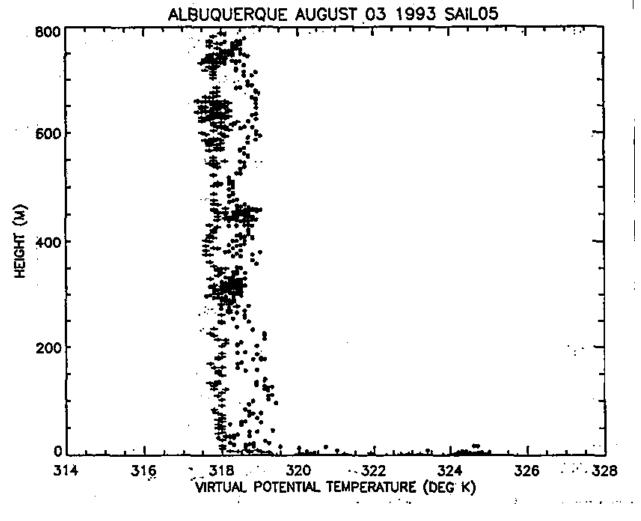


Image courtesy of AMS.

Radiative equilibrium is unstable in the troposphere Re-calculate equilibrium assuming that tropospheric stability is rendered neutral by convection:

#### **Radiative-Convective Equilibrium**

